

**Mid-Semester Test**  
**Soft Computing Applications: CS60108**  
*Spring Semester – 2023*

Full Marks: 60

Time: 2 hours

Answer **ALL** Questions

**Q. 1**

Suppose, *age* is defined over a set of real numbers in the range [0...100]. Three fuzzy sets *Young*, *MA* and *Old* are defined with their respective membership functions given below.

$$\begin{aligned} \text{Young}(x) = \{ & \\ & 1, \text{ if } \text{age}(x) \leq 25, \\ & (35-\text{age}(x))/10, \text{ if } 25 < \text{age}(x) \leq 35, \\ & 0, \text{ if } \text{age}(x) > 35 \\ & \} \end{aligned}$$

$$\begin{aligned} \text{MA}(x) = \{ & \\ & 0, \text{ if } \text{age}(x) \leq 25, \\ & 1 - (47.5-\text{age}(x))/22.5, \text{ if } 25 < \text{age}(x) \leq 47.5, \\ & 70-\text{age}(x)/22.5, \text{ if } 47.5 < \text{age}(x) \leq 70 \\ & \} \end{aligned}$$

$$\begin{aligned} \text{Old}(x) = \{ & \\ & 0, \text{ if } \text{age}(x) \leq 65, \\ & 1-(75-\text{age}(x))/10, \text{ if } 65 < \text{age}(x) \leq 75, \\ & 1, \text{ if } \text{age}(x) > 75 \\ & \} \end{aligned}$$

Find the fuzzy sets for the following:

- Not Old
- Either Young or MA
- Neither Young nor Old

[3+3+4]

**Q. 2**

Given the following rule:

IF *resistance is High* THEN *current is Low*

Also, given the following relational matrix:

$$R = \begin{matrix} & & 150\text{mA} & 50\text{mA} & 10\text{mA} \\ \begin{matrix} 10\text{K} \\ 50\text{K} \\ 100\text{K} \end{matrix} & R = & \begin{bmatrix} 0.8 & 0.7 & 0.9 \\ 0.6 & 0.4 & 0.3 \\ 0.2 & 0.5 & 0.1 \end{bmatrix} \end{matrix}$$

Suppose, the membership distribution of very high (VH) resistance is given by

$$\mu_{VH}(\text{resistance}) = \{(10K, 0.7), (50K, 0.8), (100K, 0.9)\}$$

Determine the membership distribution of very low (VL) current (i.e.,  $\mu_{VL}(\text{current})$ ) from the above data.

[10]

**Q. 3**

Suppose, we have a universe of integers,  $Y = \{1, 2, 3, 4, 5\}$ . We define the following linguistic terms as mapping onto Y:

$$\text{"Small"} = \{(1, 1), (2, 0.8), (3, 0.6), (4, 0.4), (5, 0.2)\}$$

$$\text{"Large"} = \{(1, 0.2), (2, 0.4), (3, 0.6), (4, 0.8), (5, 1)\}$$

Construct the following phrase (as a fuzzy set, say A) with the help of the above linguistic terms with hedges:

*"not very Small and not very, very Large"*

[2+3+5]

**Q. 4**

- Draw the schematic diagram of the simple model of perception. Clearly indicates what are the unknown parameters in your model. [2+1]
- The following is a training set for a 2-class (as 0 and 1) classification problem. Iterate the perceptron through the training set and obtain the weights. The algorithm which you followed preferably be stated before. You may make a reasonable assumption if any.

INPUT		OUTPUT
$X_1$	$X_2$	Y
0.25	0.353	0
0.25	0.471	1
0.50	0.353	0
0.50	0.647	1
0.75	0.705	0
0.75	0.882	1
1.0	0.705	0
1.0	1.0	1

[3+4]

**Q. 5**

- Clearly draw the Vanilla neural network with all hyperparameters in it. [4]
- Explain the Steppes descent method and hence the delta rule to learn an unknown parameter in the network. [4]
- Give a detailed account of all layers in the Vanilla neural network in terms of their input and output. [3×2]
- Following the Back propagation algorithm, derive the modified values of  $v_{ij}$  and  $w_{jk}$ , where  $v_{ij}$  denotes the weight of the connection between the  $i$ -th perceptron in the input layer to the  $j$ -th perceptron in the hidden layer and  $w_{jk}$  denotes the weight of the connection between the  $j$ -th perceptron in the hidden layer to the  $k$ -th perceptron in the output layer. [3+3]

[3+3]